GPU Font Rendering
Current State of the Art

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Terathon Software
About the speaker

- Working in game/graphics dev since 1994
  - Previously at Sierra, Apple, Naughty Dog

- Current projects:
  - Slug Library, C4 Engine, The 31st, FGED
About this talk

- Unicode
- Glyphs
- TrueType
- Font Rendering
- Typography
Unicode

- Defines character codes
- Originally 16-bit
- Now has range \(0x000000 - 0x10FFFF\)
- Divided into 17 “planes”
Basic Multilingual Plane

- 0x0000 – 0xFFFF
- First 128 code points are ASCII
- Lots of other common scripts/languages
- Lots of common symbols
Supplementary Multilingual Plane

- \(0x010000 \text{ – } 0x01FFFF\)
- Rare characters from many languages
- Rare scripts like Cuneiform and Hieroglyphs
- Mathematical symbols and bold / italic
- Emoticons 🧡
Supplementary Multilingual Plane

As of Unicode 10.0

- Non-Latin European scripts
- African scripts
- Middle Eastern and Southwest Asian scripts
- South and Central Asian scripts
- Southeast Asian scripts
- East Asian scripts
- American scripts
- Hieroglyphs
- Notational systems
- Symbols
- Unallocated code points
Supplementary Ideographic Plane

- 0x020000 – 0x02FFFF
- Less common CJK ideographs
Supplementary Ideographic Plane

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- CJK characters
- Unallocated code points

As of Unicode 10.0
Other Planes

- Planes 0x03 – 0x0D unused
- Plane 0x0E contains special tags and variation selectors
- Planes 0x0F and 0x10 for private use only
Character Encoding

- ASCII
- UCS-2 (Universal Coded Character Set)
  - Always 16 bits per character
- UTF-16
  - 16 bits or 32 bits per character
- UTF-32
  - Always 32 bits per character
UTF-8

- 1 – 4 bytes per character
  - Using variable-length encoding
- Values 0x00 – 0x7F identical to ASCII
- High bit set indicates part of multi-byte sequence
UTF-8

- 1 byte: 0x00 – 0x7F
- 2 bytes: 0x0080 – 0x7FFF
- 3 bytes: 0x0800 – 0xFFFFF
- 4 bytes: 0x10000 – 0x10FFFF
Glyphs

- Fonts contain glyphs
- Glyphs have font-specific internal numbering
- Fonts contain tables that map character codes (Unicode values) to glyph indexes
Glyphs

• Fonts typically contain many more glyphs that are not directly mapped from characters
  • Type variations
  • Alternate styles
  • Ligatures, ZWJ sequences
  • Initial, medial, final forms (Arabic)

• More about these later
TrueType

- Contains resolution-independent representations of glyph outlines
- Has character-to-glyph mappings
- Usually contains several other tables with typographic information (e.g., kerning)
Glyph Outline

- Glyph defined by one or more closed contours
- Each contour defined by continuous sequence of quadratic Bézier curves
- Winding number determines whether a given point is inside the glyph
Winding Number

- Contours defining outer edge of glyph wound in one direction (either CW or CCW is okay)

- Contours defining a hole in the glyph wound in the opposite direction
Winding Number

- Count number of positive loops for outer contours
- Subtract number of negative loops for inner contours
- Nonzero means point inside glyph boundary
Glyph Outline / Winding Number
Font Rendering in Games

- Text rendered in lots of places
  - GUI: Buttons, menus, ...
  - HUD: Score, health, ammo, ...
  - In scene: Signs, labels, computer screens, ...
  - Debug info: Console, stats, timings, ...
Basic GPU Font Rendering

- Rasterize each glyph on CPU and store results in a texture map called an “atlas”
- Can be done for multiple font sizes at once
- Packing methods can vary in sophistication
Font Atlases

Image credit: freetype-gl
Font Atlases

- Render one quad for each glyph
- Texture map the glyph’s image from the atlas
- Very simple and stupid fast
Font Atlases

- Very limited quality
- Only looks good at originally rendered size
- Magnification looks terrible
Font Atlases

- Minification also problematic
- Mipmaps work to a degree
- Glyphs must be surrounded by empty space in atlas to prevent bleeding into neighbors
Signed Distance Fields

- Instead of storing glyph images in atlas, store distance to glyph outline at each point

Image credit: Konstantin Käfer, "Drawing Text with Signed Distance Fields in Mapbox GL", 2014.
Signed Distance Fields

- Render linear coverage by scaling distance to pixel units and clamping

- Requires derivatives in pixel shader and extra computation

- Still very fast
Signed Distance Fields

- Addresses magnification problem
- Also allows good perspective rendering

Image credit: Chris Green, "Improved Alpha-Tested Magnification for Vector Textures and Special Effects", 2007.
Signed Distance Fields

- Need high resolution to capture glyph details
- Sharp corners always rounded off
  - Can be addressed with multiple distance channels
- Minification becomes bigger problem
  - Because one distance value can’t account for multiple curves in scaled-down field
Signed Distance Fields

Resolution Independence

- Render directly from original outline data
  - Control points for quadratic Bézier curves

- No more texture atlases!
  - No resolution-dependent approximation
  - Impossible to lose detail
Loop-Blinn Method

- Creates a triangulation for each glyph using its outline control points
- Each triangle corresponds to one Bézier curve
- Simple calculation based on interpolated texture coordinates yields inside/outside state
Loop-Blinn Method
Loop-Blinn Method

- Needs further subdivision for interior triangles so they never border more than one curve

- Correct antialiasing also requires more triangles in the exterior
  - Consider a pixel intersecting the outline but without its center covered by a triangle
Loop-Blinn Method

Loop-Blinn Method

- Requires a large number of triangles for each glyph
- More complex glyphs could require 1000s!
- Calculation of triangles is complex
Loop-Blinn Method

- Produces high-quality magnification

- However, minification is poor
  - Any pixel is covered by at most one triangle
  - Each triangle corresponds to only one curve
  - Thus, it’s impossible for one pixel to consider contribution from multiple nearby curves
Dobbie Method

- Covers each glyph with a single quad
- Pixel shader considers subset of all Bézier curves to determine winding number
- Basically ray tracing glyphs
Dobbie Method

- For a given point, shoot a ray outward and count curve intersections
- An intersection makes a positive or negative contribution based on its winding direction
- Nonzero total means inside glyph boundary
Dobbie Method

- Antialiasing possible along ray direction
- If intersection occurs within pixel, it makes a fractional contribution
- Test rays in multiple directions and average to get isotropic antialiasing
Dobbie Method
Dobbie Method

- Very slow to test all Bézier curves defining the glyph for each ray
- Dobbie method divides glyph’s bounding box into cells
- Each cell has list of intersecting curves
Dobbie Method

Dobbie Method

- Pixel footprint could overlap multiple cells
  - Have to sort that out in pixel shader

- Need to precompute whether cell center inside or outside glyph boundary
  - Then trace extra ray from pixel location to cell center to fix up winding number
Dobbie Method

- There's a serious problem:

- Numerical robustness

- Floating-point round-off error causes rendering artifacts
Dobbie Method

Sparkle / streaking artifacts
Glyphy

- Similar to Dobbie method in that a glyph is covered by a single quad
- Pixel shader determines distance to nearest Bézier curve
Glyphy

- Original outlines not preserved
- Also has numerical robustness problems
Glyphy

Straight lines rounded

Sparkle artifacts
Slug Library

- The result of my own research begun in 2016
- Uses one quad per glyph
- Calculates winding number in pixel shader
- Has *perfect* numerical robustness
Numerical Robustness

- Round-off errors in previous methods:
  - Generally come from determining whether roots of ray-curve intersections fall in $[0,1]$ range
  - Problems typically occur at the endpoints
  - Especially bad when ray nearly tangent to curve
  - Hacks like using epsilons or perturbing coordinates just shift the problem cases around
Numerical Robustness

- Only way to solve is to completely eliminate the [0,1] range test
-Slug introduces an equivalence class algorithm
  - Equivalence class represents control point state
  - Same actions taken for all cases in same class
Equivalence Classes

- With respect to a given ray, a particular quadratic Bézier curve is classified into one of 8 possible equivalence classes.

- Based on which side of ray each of three control points falls, positive or negative.
  - Exactly on ray is considered positive.
# Equivalence Classes

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Equivalence Classes

• For each Bézier curve, always calculate roots

\[(y_1 - 2y_2 + y_3)t^2 - 2(y_1 - y_2)t + y_1\]

\[t_1 = \frac{b - \sqrt{b^2 - ac}}{a} \quad \text{and} \quad t_2 = \frac{b + \sqrt{b^2 - ac}}{a}\]

\[a = y_1 - 2y_2 + y_3 \quad b = y_1 - y_2 \quad c = y_1\]
Equivalence Classes

- A 16-bit LUT tells us what to do with roots for each equivalence class (8 classes x 2 roots)

- Action taken only when $x$ coordinate positive at a root, meaning intersection was on ray
Winding Number

- 1 in LUT for first root means add one
- 1 in LUT for second root means subtract one
- Total after considering all curves is winding number at pixel location
- Fractional values used when roots within pixel distance of ray origin
Antialiasing

- Result is coverage value with perfect one-dimensional antialiasing
- Evaluate horizontal and vertical rays
- Combine to produce 2D antialiasing
Banding

- For best performance, we want to minimize number of curves tested

- Cells don’t work well
  - Pixel footprint can cover multiple cells
  - Pixels get larger as font size decreases
Banding

- Instead of cells, use horizontal and vertical bands that extend to infinity
Banding

- Bézier curves are sorted into the bands
  - A curve can belong to multiple bands
  - When rendering, band selected based on ray origin

- Doesn’t matter how large pixel footprints get
  - Only matters in ray direction
  - Band parallel to ray extends forever
Banding

- Curves in each band are sorted to allow early exit in pixel shader
- Once right-pointing ray’s origin is beyond maximum curve x coordinate, we’re done
Banding

- Curves sorted in both directions
- Ray points left or right depending on pixel position within a band
- Reduces number of curves tested
Bandung

- We want worst-case band to contain fewest curves possible

- GPU thread coherence will make shader wait for longest number of loop iterations in a group of pixels (32 or 64)
Bandung

- Use large number of bands
- Merge those with equal subsets of Bézier curves
Minification

- High-quality minification achieved with adaptive supersampling
  - Based on screen-space derivatives

- Already have perfect 1D antialiasing
  - Take $n$ samples in $x$ and $y$ directions
  - Produces better than $n \times n$ supersampling
Minification
Font Data

- Two texture maps, data only (no images)
- Curve texture, 4 x 16-bit float
  - Contains all Bézier curves
- Band texture, 4 x 16-bit integer
  - Contains curve subsets for all bands
Multicolor Glyphs

- Microsoft fonts use vector data for color emoji
- Layered glyphs with color palette
- Easy to handle with loop in pixel shader
Typography

- Slug algorithm can make individual glyphs look great at any scale or from any perspective
- Higher-level:
  Make entire lines of text look good
Metrics

The image illustrates the concept of metrics in font rendering, showing a letter 'A' and its bounding box. The bounding box is defined by the coordinates (0,0) and (1,1), with the advance width indicated by the horizontal distance between these points. The 'em square' is a reference unit for font metrics.
Metrics

em size
baseline
leading
baseline
cap height
ascent
ex height
descent

ABCXYZ
abcxyz
Kerning

- Some pairs of glyphs appear to the eye to have too much space in between

- Fonts usually contain kerning tables to improve overall appearance
Kerning

“Too Wavy.”

“Too Wavy.”

Kerning off

Kerning on
Ligatures

- Replaces a sequence of glyphs with one new glyph that looks better

- In some languages, ligatures that change appearance are required for correctness
Ligatures

The firefly craft. The firefly craft.

Normal text

With ligatures
ZWJ Sequences

- Unicode has control character “zero-width joiner” (ZWJ)

- Often used by fonts for combining several glyphs into single ligature
ZWJ Sequences
Combining Marks

- Unicode defines many accents and other symbols that are designed to combine with a preceding base character

- Fonts determine how this combination works by defining attachment points
Combining Marks

\[ \text{a} \text{̈} \quad \text{á} \]
Alternate Substitution

- OpenType fonts define a large array of substitution features
- Independent of Unicode
- Not directly accessible through characters
Alternate Substitution

- Small caps
- Subscripts and superscripts
- Case-sensitive forms
- Stylistic alternates
- Tabular and proportional figures
- Lining and old-style figures
Small Caps

Text

Text

Small caps alternates

Scaled glyphs
Lining and Old-style Figures

0123456789

0123456789
Cursive Joining

- In languages like Arabic, letters have multiple forms depending on position in word
- Isolated, initial, medial, final forms
- Do not have separate character codes
Cursive Joining

متدمة تقدير الخط وتخطيط النص

متقدمة تقدير الخط وتخطيط النص
Materials

- Rendering glyphs outputs coverage value
  - (Plus color for multi-color emoji)

- Can be combined with other materials in game
Materials
Contact / More Info

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- Twitter: @EricLengyel
- sluglibrary.com